

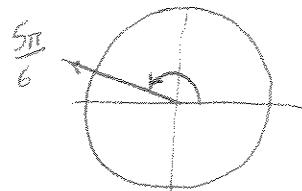
M1060-2 QUIZ 1 (Spencer Stirling) - September 2, 2010

Directions: You may attach more sheets if necessary. SHOW ALL WORK and CLEARLY mark your solutions.

- 1) (4 points) Find at least two coterminal angles to the angle given, and sketch the angle on the unit circle

(a) $\frac{5\pi}{6}$ coterminal angles (there are many)

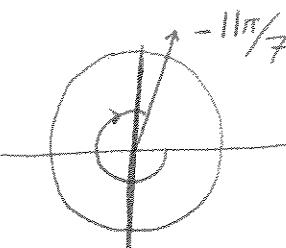
$$\frac{5\pi}{6} + 2\pi = \frac{5\pi}{6} + \frac{12\pi}{6} = \boxed{\frac{17\pi}{6}}$$



$$\frac{5\pi}{6} - 2\pi = \frac{5\pi}{6} - \frac{12\pi}{6} = \boxed{-\frac{7\pi}{6}}$$

(b) $-\frac{11\pi}{7}$ coterminal angles

$$-\frac{11\pi}{7} + 2\pi = -\frac{11\pi}{7} + \frac{14\pi}{7} = \boxed{\frac{3\pi}{7}}$$



$$-\frac{11\pi}{7} - 2\pi = -\frac{11\pi}{7} - \frac{14\pi}{7} = \boxed{-\frac{25\pi}{7}}$$

- 2) (2 points) Convert each angle into radians. Leave your answer in terms of π (i.e. do NOT use a calculator)

(a) 315°

$$(315^\circ) \left(\frac{\pi}{180^\circ} \right) = \frac{315}{180} \pi = \frac{105}{60} \pi = \boxed{\frac{21}{12} \pi}$$

(b) -144°

$$(-144^\circ) \left(\frac{\pi}{180^\circ} \right) = \boxed{-\frac{4}{5}\pi}$$

- 3) (2 points) Convert each angle into degrees. Leave your answer in terms of a fraction (i.e. do NOT use a calculator)

(a) $\frac{7\pi}{3}$

$$\left(\frac{7\pi}{3}\right) \left(\frac{180^\circ}{\pi}\right) = \boxed{420^\circ}$$

(b) $-\frac{34\pi}{15}$

$$\left(-\frac{34\pi}{15}\right) \left(\frac{180^\circ}{\pi}\right) = \cancel{(-34)(12^\circ)} = \boxed{-408^\circ}$$

4) (6 points) A car is moving at a speed of 65 miles per hour, and the diameter of its wheels is 2.5 feet. Recall that there are 5280 feet in a mile.

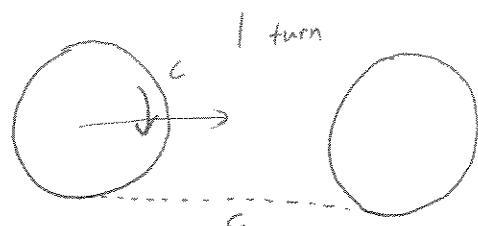
- (a) Find the number of revolutions per minute (RPM) that the wheels are rotating
- (b) Find the angular speed of the wheels in radians per second

$$\textcircled{a} \quad (65 \frac{\text{miles}}{\text{hr}}) \left(\frac{5280 \text{ ft}}{1 \text{ mile}} \right) \left(\frac{1 \text{ hr}}{60 \text{ min}} \right) = 5720 \text{ ft/min} \leftarrow \begin{array}{l} \text{65 mph converted} \\ \text{min} \qquad \qquad \text{to ft/min} \end{array}$$

1

$$\text{circumference } c = \pi d = (\pi) 2.5 \text{ ft} = 2.5\pi \text{ ft} = c$$

In one full turn of wheel car travels c distance



~~1 revolution $\approx 2.5\pi \text{ ft}$~~
so car travels $\frac{2.5\pi \text{ ft}}{1 \text{ revolution}}$

~~# revolutions/min~~

$$\text{so } \frac{\# \text{ revolutions}}{\text{min}} = \left(\frac{5720 \text{ ft}}{\text{min}} \right) \left(\frac{\text{revolution}}{2.5\pi \text{ ft}} \right) \approx \boxed{728.3 \frac{\text{rev}}{\text{min}}}$$

b) convert to $\frac{\text{rad}}{\text{sec}}$

$$\omega = \left(728.3 \frac{\text{revolutions}}{\text{min}} \right) \left(\frac{2\pi \text{ rad}}{\text{revolution}} \right) \left(\frac{1 \text{ min}}{60 \text{ sec}} \right) =$$

$$\boxed{\omega = 76.3 \frac{\text{rad}}{\text{sec}}}$$